New Mathematical Methods for Complex System in Ecology: Summary and Outlook

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- Environmental problems are becoming more difficult and are now more pressing
 - Global climate change
 - Environmental degradation
 - Invasive species
 - Overfishing
 - Emerging diseases
 - ...

- We are getting much more data and we need models (and math) to try to make sense out of it.
 - Satellite tracking
 - Drones
 - New genetic methods (eg, bar coding)

- There are many key problems we are only just starting to solve and we now need new and improved methods
 - Full characterization of transient dynamics
 - Robust theory of how to connect dynamical models to ecology and fit the models to data
 - Tipping points arising from environmental change
 - Dynamical systems with intermediate levels of noise
 - The list goes on...

We need new theoretical and computational frameworks to understand the problems and to connect to data

- Structural sensitivity (Andrew)
- Tipping points, critical transitions and factors that affect them (Sebastian W, Christian)
- "Stability" of ecological states under stochasticity (Karen)
- Impact of stochasticity on structured populations (Sebastian S)
- Optimal responses to complex environmental problems, and how to incorporate data (Suzanne)

We need new theoretical and computational frameworks to understand the problems and to connect to data

- How to fit complex models to data with observation error and make biological or management inferences (Steve, Natalia, Rebecca)
- Evolution in spatial systems (Chris)
- Unexpected complex nonlinear outcomes from simple models (Bob)
- Transient dynamics (Frithjof, Sergei, Susmita)
- Ecosystem functioning under stressful conditions (Ehud)
- Early warning metrics (Vasilis)

- Mathematical methods developed for ecology have "spin-off" effects and synergies on mathematics
 - There is a long history of challenging math ecology problems giving rise to new mathematics
 - We need to develop new math based on the ecology in addition to borrowing old math









Recurring themes involving <u>New Mathematics</u>

- Nonlinear dynamical systems
- Multiple time scales
- Bifurcation analysis/energy potentials
- Stochastic processes
- Inference/data analysis methods
- Perturbed dynamics (ranging from one-time to continual)
- Meta-analysis
- Optimization and control
- Spatial complexities
- Other?

What are key advances in <u>Theoretical Ecology</u> coming from new math?

- A theory for tipping points for ecological systems
- A theory for transients for ecological systems
- A new understanding of the roles of sensitivity (structural and parameter) and identifiability (structural and applied) in determining which questions we can reasonably answer
- Ecosystem management and decision making
- Other?

What are some key <u>Environmental or</u> <u>Ecological Applications</u> for the new math?

- Predicting effect of environmental change on ecological dynamics (non-stationary)
- Enhanced environmental forecasting for populations (eg., fisheries)
- Feedback between ecology and management (humanenvironment systems)
- Methods for ecological data analysis
- Other?

What are some of the biggest <u>Mathematical</u> <u>Gaps</u> that we could fill in?

- Intermediate asymptotics for stochastic processes (non-ergodic) and the possibility of long-term transient dynamics
- Extending "r-tipping" theory to more complex systems (eg, predatorprey, spatial problems via PDEs and so on)
- A more complete theory for model sensitivity for inverse problems
- A more complete theory of parameter identifiability for dynamical systems
- Further development of methods for analysis of transient dynamics
- Dynamical systems on complex networks
- Other?

Are there some questions that it doesn't make sense to try to try answer?

- Mathematical analysis of structural sensitivity can help us determine which these questions might be.
- Mathematically showing what you cannot do could be as useful as showing what you can
- A solution might lie in either reformulating questions or possibly by applying nonparametric models
- Other approaches?

Questions/Comments?

Thank you on behalf of the organizers: Andrew, Alan and Mark

- It has been a fun week
- You have made it really easy for us to be organizers
- Thanks to BIRS for a great set up, great food (and great weather!)
- BIRS also supports Focused Research Groups (up to 8 people) for periods of one to two weeks
- If you would like to, please email your workshop comments/testimonial to <u>birs@birs.ca</u>